



models from fluid dynamics. In the end, we introduce adaptive time stepping from a control theory viewpoint to accelerate simulations evolving on different scales in time.

The target group are master students that are interested in applied mathematics, numerical simulation, fluid dynamics, or control theory.

## Contents

part I:

1. Motivation
2. Introduction to kinetic theory
3. The method of moments
4. Nonlinear moment framework
5. Nonlinear moment equations for rarefied gases
6. Hyperbolic moment equations for rarefied gases
7. Filtered moment models
8. Hilbert expansion-based model reduction
9. Moment equations for shallow flows
10. Moment models for Uncertainty Quantification
11. Other model reduction techniques

part II:

- 1 Examples for Multi-scale systems
- 2 Finite Volume schemes
- 3 Standard methods for stiff models
- 4 Multi-scale methods for stiff models
- 5 Structure-preserving methods
- 6 Adaptive Time stepping

## Initial competences

Assumed knowledge: differential equations numerical methods, e.g., as in Numerical Analysis, Mathematical Modelling

## Final competences

At the end of the course, the student is able to:

1. apply different model reduction techniques to derive macroscopic PDEs from an underlying micro-/mesoscopic PDE description.
2. analyze properties like stability and hyperbolicity of the models.
3. use reduced models to solve application problems, e.g. from the fields of rarefied gases or free-surface flows.
4. choose from a variety of tailored methods to solve multi-scale hyperbolic PDEs.
5. understand the properties, advantages and disadvantages of the discussed numerical schemes.

## Conditions for credit contract

Access to this course unit via a credit contract is determined after successful competences assessment

## Conditions for exam contract

This course unit cannot be taken via an exam contract

## Teaching methods

Seminar, Lecture

## Extra information on the teaching methods

Ufora will be used.

The learning material will be provided in English.

## Study material

Type: Syllabus

Name: Lecture notes on Model Reduction and Multiscale Numerical Methods

Indicative price: Free or paid by faculty

Optional: no

Language : English

Number of Pages : 200

Available on Ufora : Yes

Online Available : No

Available in the Library : No

Available through Student Association : No

### **References**

lecture notes will be provided

### **Course content-related study coaching**

The students can make appointments with the lecturer to have extra individual coaching.

### **Assessment moments**

end-of-term and continuous assessment

### **Examination methods in case of periodic assessment during the first examination period**

Presentation, Written assessment

### **Examination methods in case of periodic assessment during the second examination period**

Presentation, Written assessment

### **Examination methods in case of permanent assessment**

Assignment

### **Possibilities of retake in case of permanent assessment**

examination during the second examination period is possible

### **Extra information on the examination methods**

End-of-term evaluation: Written assessment (project report) and presentation

Permanent evaluation: (bi-)weekly homework assignments

### **Calculation of the examination mark**

Continuous (30%) and end-of-term assessment (70%)