Mathematical Modelling of Fuzziness (C004370)

Course size *(nominal values; actual values may depend on programme)*

Credits 6.0 **Study time** 165 h

Course offerings and teaching methods in academic year 2023-2024

| A (semester 1) | Dutch | Gent | lecture |
| | | | seminar |

Lecturers in academic year 2023-2024

| Cornelis, Chris | WE02 | lecturer-in-charge |

Offered in the following programmes in 2023-2024	**crdts**	**offering**
Master of Science in Teaching in Science and Technology(main subject Mathematics)	6	A
Master of Science in Mathematics	6	A

Teaching languages

Dutch

Keywords

Order structures, algebraic structures for many-valued logics, fuzzy logic, fuzzy sets, calculus of fuzzy quantities, fuzzy inference

Position of the course

Many complex problems cannot be solved by a sharp analysis based on classical logic and the corresponding set theory. In case of increasing complexity a level is quickly reached above which accuracy and relevance counteract each other. A possible solution to these problems is to abandon the idea of accuracy and allow imprecision and partial certainties. The scientific literature of the last decade introduces many new models for representing imprecision and uncertainty. The most important of these is the theory of fuzzy sets. The usefulness of this theory is confirmed by the massive demand for patents by Japanese companies for products based on fuzzy set theory. In this course we will introduce the basic principles and discuss some applications of this new theory, and thus introduce the student to a recent domain of applicable mathematics.

Contents

- Auxiliary order and algebraic structures (poset, lattice, Boolean algebra, Morgan algebra, …)
- Logical operators on the unit interval (negators, triangular norms and conorms, implicators)
- Algebraic structures for many-valued logic calculi (residuated lattices, MTL algebra's, BL algebra's, MV algebra's, Heyting algebra's)
- Formal fuzzy logic
- Fuzzy sets, flou sets and L-fuzzy sets
- Calculus of fuzzy quantities and fuzzy numbers
- Degree of inclusion, similarity and fuzziness
- Fuzzy quantifiers
- Possibility theory and fuzzy inference

Initial competences

No particular mathematical prerequisites. Obviously a positive attitude towards mathematics and formal logic is needed.

Final competences

1 Students should be familiar with the basic concepts and techniques from fuzzy

set theory and related models of uncertainty among them L-fuzzy set theory and flou set theory.

2 Students should be ready to start more advanced courses offered in the master of computer science and the master of applied mathematics.

Conditions for credit contract

Access to this course unit via a credit contract is determined after successful competences assessment

Conditions for exam contract

This course unit cannot be taken via an exam contract

Teaching methods

Seminar, Lecture

Extra information on the teaching methods

The theory is taught during the lectures. During the labs, the students solve exercises with the help of a teaching assistant. For the independent work, the students prepare an exercise or a theoretical topic and present it during class.

Learning materials and price

The learning material is available in electronic form on the course website on Ufora.

References

- E.E. Kerre: Introduction to the Basic Principles of Fuzzy Set Theory and Some of its Applications, second revised edition. Communication & Cognition, Gent (1993).
- E.P. Klement, R. Mesiar, E. Pap, Triangular Norms, Kluwer Academic Publishers (2000).

Course content-related study coaching

Students actively process the learning material while making exercises in the presence of a teaching assistant. Furthermore students can submit their solutions for additional exercises to get feedback from the assistant or the instructor. The assistant and the instructor are also available to students for additional individual explanation outside of the scheduled class times.

Assessment moments

end-of-term and continuous assessment

Examination methods in case of periodic assessment during the first examination period

Written assessment

Examination methods in case of periodic assessment during the second examination period

Written assessment

Examination methods in case of permanent assessment

Assignment

Possibilities of retake in case of permanent assessment

not applicable

Calculation of the examination mark

Combination of non-periodical evaluation (written report and oral presentation of the assignment, i.e. 40% of the final score) and periodical evaluation (written exam, i.e. 60% of the final score).
To be able to pass, a student should obtain a score of at least 10/20 for the exam.