

## Relativistic Hydrodynamics - from Quantum Field Theory to Black Holes (C004421)

**Course size** *(nominal values; actual values may depend on programme)*

**Credits 6.0**                      **Study time 180 h**

**Course offerings and teaching methods in academic year 2025-2026**

null

**Lecturers in academic year 2025-2026**

Heller, Michal	WE05	lecturer-in-charge
Serantes Rubianes, Alexandre	WE05	co-lecturer

**Offered in the following programmes in 2025-2026**

null

**crdts                      offering**

**Teaching languages**

English

**Keywords**

Relativistic hydrodynamics, Schwinger-Keldysh formalism, kinetic theory, applied holography, black holes, quark-gluon plasma, heavy-ion collisions

**Position of the course**

The goal of this course is to teach both fundamental concepts, as well as recent developments in non-equilibrium field theory centred around relativistic viscous hydrodynamics, its microscopic origins and questions of its applicability. This is a timely topic due to experimental studies of collective state of strong interactions — the quark-gluon plasma — at RHIC and LHC accelerators in the course of the past 20 years and associated theoretical progress. The course provides an opportunity for students to deepen their knowledge of quantum field theory by studying it in the context of collective states of matter. In a similar vein, it provides also an opportunity to train general relativity skills by studying a novel paradigm (holography) in which time-dependent black hole processes describe nonequilibrium physics of strongly-coupled quantum field theories. Finally, the students will familiarise themselves with the notion of asymptotic expansions, usually known from the perturbation theory in quantum systems, by studying their appearance in the context of non-equilibrium physics.

**Contents**

- Introduction
- Basics of relativistic hydrodynamics
- Relativistic hydrodynamics as an initial value problem
- Viscosity from the Kubo formula and the Schwinger-Keldysh formalism
- Black holes as a novel tool to study strongly-coupled quantum field theory
- From weakly-coupled quantum field theory to relativistic kinetic theory
- Nonequilibrium processes beyond relativistic hydrodynamics
- Relativistic hydrodynamics and asymptotic series
- Summary and discussion of some open problems in this discipline

The course will require students to participate in small groups in projects based on literature review (for example, new formulations of equations of motion for relativistic hydrodynamics, action formulations of relativistic hydrodynamics, cutting-edge applications of asymptotic series to relativistic hydrodynamics, relativistic hydrodynamics and fluctuations, higher derivative modifications of general relativity and insights from relativistic hydrodynamics, retarded correlators

in free quantum field theory, hydrodynamic attractors) or simple research (for example, solving equations of relativistic hydrodynamics or simple relativistic kinetic theory numerically, studying asymptotic series for relativistic hydrodynamics in a novel setting, study of hydrodynamic attractors in a novel setting).

### **Initial competences**

Required "Quantum field theory" and Relativity, useful but not required Quantum Black Holes and Holography

### **Final competences**

- 1 Understanding of the relevance of relativistic hydrodynamics for modern theoretical physics.
- 2 Understanding of the challenges posed by nonequilibrium physics of interacting quantum field theories.
- 3 Working knowledge of relativistic hydrodynamics and related topics that reflects their contemporary understanding.
- 4 Enhancement of understanding of other important contemporary theoretical physics topics, such as asymptotic series, effective field theory or modifications of general relativity, via their appearance in the context of relativistic hydrodynamics.
- 5 Building or strengthening the ability to a) read scientific papers discussing current developments in theoretical physics and b) start research in this area, or in theoretical physics in general.
- 6 Building or strengthening the ability to work in a group with a focus on scientific collaboration.
- 7 Building or strengthening the ability to present the results of group research (which includes scientific writing).

### **Conditions for credit contract**

Access to this course unit via a credit contract is determined after successful competences assessment

### **Conditions for exam contract**

This course unit cannot be taken via an exam contract

### **Teaching methods**

Seminar, Lecture, Independent work

### **Extra information on the teaching methods**

Project: students form teams to prepare a literature review or participate in a computational exercise.

Teams present their outcomes both in the form of reports, as well as presentations.

### **Study material**

None

### **References**

Freely available on the web:

<https://arxiv.org/abs/1205.5040>

<https://arxiv.org/abs/0909.0518>

<https://arxiv.org/abs/1707.02282>

<https://arxiv.org/abs/1712.05815>

### **Course content-related study coaching**

Outside lecture hours, the teacher will be available for further explanation during consultation hours and upon an appointment.

### **Assessment moments**

end-of-term and continuous assessment

### **Examination methods in case of periodic assessment during the first examination period**

Oral assessment

**Examination methods in case of periodic assessment during the second examination period**

Oral assessment

**Examination methods in case of permanent assessment**

Assignment

**Possibilities of retake in case of permanent assessment**

examination during the second examination period is possible

**Calculation of the examination mark**

- 35% continuous assessment (project)
- 65% end-of-term evaluation (oral examination)